



### SCHOOL on Generation IV reactors fuel cycle

### Thermodynamic aspects of nuclear fuels (Modelling)

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### Outline

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- 2 Basic Gibbs energy models
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# The Gibbs energy

• The Gibbs energy of a system is defined by:

$$G = H - T S = U + PV - T S$$



Josiah Willard Gibbs (1839-1903)

- *H* is the enthalpy  $\Rightarrow$  heat content of the system
- *T* is the temperature
- *S* is the entropy of the system ⇒ randomness of the system
- U is the internal energy of the system  $\Rightarrow$  kinetic and potential energies of atoms
- *P* is the pressure
- *V* is the volume

- vibrations bonds
- G is the key function in thermodynamics of materials
- At constant temperature and pressure, a closed system (fixed mass and composition) will be in stable equilibrium if it has the lowest value of the Gibbs energy:

$$dG = 0$$

# Thermodynamic equilibrium

• 
$$G = H - T S$$

⇒Compromise between low enthalpy and high entropy



 $\Rightarrow$  The A configuration is the lowest possible value of  $G \Rightarrow$  Equilibrium

⇒The B configuration is a metastable equilibrium state (local equilibrium)

⇒The intermediate configurations are unstable

⇒The rate at which the system will reach the equilibrium is not provided by thermodynamics

### The Gibbs energy

#### ⇒ Thermodynamic potential at given P, T, n

$$G = U + PV - TS = H - TS$$

• H = U + PV $\rightarrow$  Enthalpy (U: internal energy)

• 
$$\left(\frac{\partial G}{\partial T}\right)_{P,N_i} = -S$$

Entropy

•  $\left(\frac{\partial G}{\partial N_i}\right)_{T,P,N_{j\neq i}} = \mu_i$  •  $C_P = -T \left(\frac{\partial^2 G}{\partial T^2}\right)_{P,N_i}$  • Heat capacity

⇒ Key thermodynamic properties to describe the phases

### **Gibbs energy minimization**

- At given *T*, *P*,  $n_i$  the equilibrium corresponds to the minimum of the Gibbs energy of the system: dG = 0
- The Gibbs energy of the system G is a linear combination of the Gibbs energies of the phases,  $G_m^{\varphi}$ :

$$G = \sum_{i} m^{\varphi} G_{m}^{\varphi}$$

 $m^{arphi}$ : mole fraction of phase arphi



#### **CALPHAD (CAL**culation of **PHA**se **D**iagram) method:

• At given T, P,  $n_i$  the equilibrium is calculated by minimization of the Gibbs energy of the system: dG = 0

➡ Coupling Gibbs energies and phase diagrams



The phase diagram can be calculated from the phases Gibbs energies

#### Calphad modeling ➡ Assessment procedure

- Mathematical functions are chosen to describe the Gibbs energy of the phases

 $G_m^{\alpha}(T, p, x_i^{\alpha} or y_k^{(l,\alpha)})$ 

- The variables are assessed by a least-square minimizing method to reproduce the available thermodynamic and phase diagram data

 For a multi-component system, the equilibrium is calculated by extrapolation from models for binary and ternary subsystems

Good prediction of
both phase diagram and phase
thermodynamic data for multi component systems



➡ SATA (School on Advanced Thermodynamic Assessment)

### Sublattice model to describe the phases

**The sublattices correspond to equivalent positions** i.e. sites belonging to the same Wyckoff position

To simplify the model, several sets of equivalent positions may be combined and treated as a single sublattice

#### A single sublattice model is used for all the phases with the same crystalline structure

FCC (Faced centered cubic)

(A)1(Va)1



**BCC (Body centered cubic)** 



#### Model for phases with a fixed composition ⇒ Pure elements, stoichiometric compounds

•  $G_m^{\alpha}$  is the molar Gibbs energy of the phase  $\alpha$ , referred to the enthalpy of the pure elements in their stable state at 298.15 K and 1 bar (SER: Stable Element Reference).

 $\Rightarrow G_m^{\alpha} - \sum_i b_i H_i^{SER} = a_0 + a_1 T + a_2 T \ln T + a_3 T^2 + a_4 T^{-1} + a_5 T^3 \dots$ 

 $\boldsymbol{b}_i$  is the stoichiometric coefficient of the element i in the phase  $\alpha$ 



### Model for a regular solution (A,B)

Influence of the interaction parameter  $L_{AB}$  on the phase diagram



### Model for a real solution (A,B)

Dependence in composition of the interaction parameter **PRedlich-Kister** 

 $G_m^{\alpha} = \mathbf{x}_A \circ \mathbf{G}_A + \mathbf{x}_B \circ \mathbf{G}_B + \mathbf{R}\mathbf{T}(\mathbf{x}_A \mathbf{ln}\mathbf{x}_A + \mathbf{x}_B \mathbf{ln}\mathbf{x}_B) + \mathbf{x}_A \mathbf{x}_B \mathbf{L}_{AB}$ 

 $\Rightarrow L_{AB} = \sum_{v=0} (x_A - x_B)^v v_{L_{AB}} = {}^0L_{AB} + {}^1L_{AB} (x_A - x_B) + {}^2L_{AB} (x_A - x_B)^2 + \dots$ 



 $^{\nu}L_{AB}=20000$ 

#### How to model the U-Pu-O system ?

#### ■1<sup>st</sup> step: modeling of the U-O, Pu-O and U-Pu binary sub-systems

- Binary interaction parameters for solutions
- G functions for the binary compounds



#### 2<sup>nd</sup> step: modeling of the U-Pu-O ternary system

- Ternary interaction parameters for solutions
- G functions for the ternary compounds



UO-

U

# Sublattice model for non stoichiometric UO<sub>2±x</sub>

■ Uranium dioxide UO<sub>2+x</sub> with fluorite structure has a large oxygen composition range



#### ■Compound Energy Formalism + Three sublattice model (U<sup>+3</sup>,U<sup>+4</sup>,U<sup>+5</sup>) (O<sup>-2</sup>,Va)<sub>2</sub> (O<sup>-2</sup>,Va)

➡ Formation of oxygen vacancies and interstitials compensated by reduction/oxidation of U<sup>+4</sup> into U<sup>+3</sup>/U<sup>+5</sup>



➡ Important parameters are: G(UO<sub>1.5</sub>), G(UO<sub>2</sub>), G(UO<sub>2.5</sub>)

[ Guéneau et al, JNM 419 (2011) 145]

### Thermodynamic properties for stoichiometric UO<sub>2</sub>

Even in stoichiometric UO<sub>2</sub>, point defects (Oxygen Frenkel pairs, electronic defects) form at high temperature



The increase in the heat capacity for T>1500 K is due to the increase in point defect concentration

### Thermodynamic data on non stoichiometric UO<sub>2±x</sub>

Experimental oxygen and uranium chemical potential data are available

 $\mu_{O_2} = \overline{\Delta G}(O_2) = R T \ln p_{O_2}$ 

$$\mu_U = \overline{\Delta G}(U) = R T \ln a_U$$





➡ The oxygen and uranium chemical potentials vary strongly with oxygen stoichiometry

## Thermodynamic data on non stoichiometric UO<sub>2±x</sub>

The oxygen potential variation is related to point defect concentration:

- O/M<2: (U<sup>+3</sup>,U<sup>+4</sup>) (O<sup>-2</sup>,Va)<sub>2</sub> (Va) ⇒ Oxygen vacancies and U<sup>+3</sup>
- O/M>2: (U<sup>+4</sup>,U<sup>+5</sup>) (O<sup>-2</sup>)<sub>2</sub> (O<sup>-2</sup>,Va) ⇒ Oxygen interstitials and U<sup>+5</sup>





[Guéneau et al, JNM 419 (2011) 145]

### Phase diagram data on the U-O system



[Guéneau et al, JNM 419 (2011) 145]

## Thermodynamic data on non stoichiometric PuO<sub>2-x</sub>

■ Plutonium dioxide PuO<sub>2-x</sub> has a large oxygen composition range with O/Pu<2



#### ■ Three sublattice model (Pu<sup>+3</sup>,Pu<sup>+4</sup>) (O<sup>-2</sup>,Va)<sub>2</sub> (Va)

#### ➡ Formation of oxygen vacancies (Va) compensated by reduction of Pu<sup>+4</sup> into Pu<sup>+3</sup>



### Phase diagram data on the Pu-O system



The experimental data on melting point data of PuO<sub>2</sub> are very scattered:

- The « reference » data (2670-2700 K) from the 60's-70's measured by thermal analysis in W crucible
- In 2005, Kato et al performed measurements (2850 K) using thermal analysis and Re crucible
- In 2010, De Bruycker et al did new measurements (3017 K) using laser heating (self-crucible)

#### $\Rightarrow \Delta T \sim 300$ K between old and recent measurements !!

➡ According to the calculations, PuO<sub>2</sub> loses oxygen below its melting point ➡ Congruent melting for O/Pu<2</p>

## Melting point data on actinide oxides

Why such large discrepancies bewteen old and new measurements ?



μ(O<sub>2</sub>) in PuO<sub>2</sub> >> μ(O<sub>2</sub>) in UO<sub>2</sub> ➡ PuO<sub>2</sub> loses oxygen at high temperature ➡ The reactivity PuO<sub>2</sub>/W is >> than for UO<sub>2</sub>/W ➡ The melting point for PuO<sub>2</sub> was underestimated due to a reaction with the crucible ➡ Laser heating with self-crucible is a suitable method

# ➡ Model for (U,Pu)O<sub>2±x</sub>

■ Mixed uranium and plutonium dioxide (U,Pu)O<sub>2±x</sub> has a large oxygen composition range



Three sublattice model (U<sup>+3</sup>, U<sup>+4</sup>, U<sup>+5</sup>, Pu<sup>+3</sup>, Pu<sup>+4</sup>) (O<sup>-2</sup>, Va)<sub>2</sub> (O<sup>-2</sup>, Va)

⇒ Ternary interaction parameters between cations have been adjusted to fit experimental data



### Experimental thermodynamic data for (U,Pu)O<sub>2±x</sub>



### Defect chemistry in (U,Pu)O<sub>2±x</sub>

#### ■ Three sublattice model (U<sup>+3</sup>, U<sup>+4</sup>, U<sup>+5</sup>, Pu<sup>+3</sup>, Pu<sup>+4</sup>) (O<sup>-2</sup>, Va)<sub>2</sub> (O<sup>-2</sup>, Va)

- For O/M<1.9: Oxygen vacancies and U<sup>+4</sup> ⇒ U<sup>+3</sup>, Pu<sup>+3</sup>
- For 1.9<O/M<2: Oxygen vacancies and Pu<sup>+4</sup> ⇒ Pu<sup>+3</sup>, U<sup>+4</sup>
- For O/M>2: Oxygen interstitials and  $U^{+4} \Rightarrow U^{+5}$

Reduction of U<sup>+4</sup>

Reduction of Pu<sup>+4</sup>

Oxidation of U<sup>+4</sup>





#### $\downarrow$ UO<sub>2</sub>-PuO<sub>2</sub> system

Phase diagram data Guéneau et al, JNM 2011 3400 3400 3300 3300 3200 3200 3100 3100 3000 3000 ≚ 2900 ¥ 2900 2800 2800 Liquidus Bohler 2014 Liquidus Bohler 2014 2700 -○ Solidus Bohler 2014  $\nabla$ 2700 -○ Solidus Bohler 2014  $\nabla$ • De Bruycker 2010 De Bruycker 2010 2600 -□ Solidus - Kato 2009 2600 -□ Solidus - Kato 2009 Liquidus - Kato 2009 Liquidus - Kato 2009 2500 -2500 -Liquidus - Lyon and Baily Liquidus - Lyon and Baily 2400 -2400 0.2 0.8 1.0 PuO2 0.6 0.4 0.2 0.6 0.8 0.4 1.0 UO2 x(PuO2) UO1.98 PuO1.96 x(PuO1.96) -Lyon and Bailey • « **Reference** » data measured by thermal analysis in **W crucible** - Kato et al Thermal analysis with Re crucible Higher solidus / liquidus T

De Bruycker et al
Laser heating
Consistent with the new melting point of PuO<sub>2</sub> (3017 K).
A minimum is found in the liquidus curve

⇒ The data of Bohler (2014) have to be taken into account to improve the model for the liquid/solid transition

### Isothermal sections of the U-Pu-O system



[Guéneau et al, JNM 419 (2011) 145]

# Thermodynamic parameters for (U,Pu)O<sub>2±x</sub>

(Pu<sup>+3</sup>,Pu<sup>+4</sup>,U<sup>+3</sup>,U<sup>+4</sup>,U<sup>+5</sup>)(O<sup>-2</sup>,Va)<sub>2</sub>(O<sup>-2</sup>,Va)

Pu-O

MOX : (Pu <sup>+3</sup> ,Pu <sup>+4</sup> ,U <sup>+3</sup> ,U <sup>+4</sup> ,U <sup>+5</sup> )(O <sup>-2</sup> ,Va) <sub>2</sub> (O <sup>-2</sup> ,Va)	$G_{(Pu^{+4})(O^{-2})(Va)}^{MOX} - H_{Pu}^{SER} - 2H_{O}^{SER} = G_{PuO_2}^{MOX} - H_{Pu}^{SER} - 2H_{O}^{SER}$
$G_{(U^{+3})(O^{-2})(Va)}^{MOX} = G_{UO_2}^{MOX} - G_{(U^{+4})(Va)(Va)}^{MOX} + G_{(U^{+3})(Va)(Va)}^{MOX}$	$= -1099562.8 + 505.428856T - 83.31922T \ln T$
$G_{(U^{+4})(O^{-2})(Va)}^{MOX} - H_U^{SER} - 2H_O^{SER} = G_{UO_2}^{MOX} - H_U^{SER} - 2H_O^{SER}$	$-0.00584178T^2 - 2.29241167.10^{-11}T^3 + 913506T^{-1}$
$= -1118940.2 + 554.00559T - 93.268T \ln T + 1.01704254.10^{-2}T^{2}$	$G_{(Pu^{*4})(Va)(Va)}^{MOX} = G_{PuO_2}^{MOX} - 2G_O^{gas}$
$-2.03335671.10^{-6}T^{3}+1091073.7T^{-1}$	$G_{(Pu^{+4})(O^{-2})(O^{-2})}^{MOX} = G_{PuO_2}^{MOX} + G_O^{gas} + 80T$
$G_{(U^{+5})(O^{-2})(Va)}^{MOX} = G_{UO_2}^{MOX} - 58351.62 + 39.67611T + 0.69315RT$	$G_{(Pu^{+4})(Va)(O^{-2})}^{MOX} = G_{PuO_2}^{MOX} - G_O^{gas} + 80T$
$\overline{G_{(U^{+3})(Va)(Va)}^{MOX}} = \overline{G_{UO_2}^{MOX}} - 2\overline{G_O^{gas}} + 747127 - 70.22618T + 1.12467RT$	$G_{(Pu^{+3})(O^{-2})(Va)}^{MOX} = G_{(Pu^{+3})(Va)(Va)}^{MOX} + 2G_O^{gas}$
$\overline{G_{(U^{+4})(Va)(Va)}^{MOX}} = \overline{G_{UO_2}^{MOX}} - 2\overline{G_O^{gas}} + 545210.5$	$G_{(Pu^{+3})(Va)(Va)}^{MOX} = 0.5 G^{Pu_2O_3} - 1.5 G_O^{gas} + 3817.7 + 1.12467 RT$
$\frac{G_{(U^{+5})(V_a)(V_a)}}{G_{(U^{+5})(V_a)(V_a)}} = G_{(U^{+5})(Q^{-2})(V_a)}^{MOX} - 2G_Q^{gas} + 700000$	$G_{(Pu^{+3})(O^{-2})(O^{-2})}^{MOX} = G_{(Pu^{+3})(Va)(Va)}^{MOX} + 3G_O^{gas} + 80T$
$\frac{G_{(U^+)(Q^-)}^{MOX}}{G_{(U^+)(Q^-)}^{MOX} - G_{(U^+)}^{MOX} - G_{(U^+)}^{MOX} + G_{Q}^{gas}}$	$G_{(Pu^{+3})(Va)(O^{-2})}^{MOX} = G_{(Pu^{+3})(Va)(Va)}^{MOX} + G_{O}^{gas} + 80T$
$G^{MOX} = G^{MOX} + G^{gas}$	$L_{(Pu^{+3},Pu^{+4})(O^{-2})(Va)}^{MOX} = L_{(Pu^{+3},Pu^{+4})(Va)(Va)}^{MOX} = +9781.9 + 3.06205T$
$G_{(U^{+4})(O^{-2})(O^{-2})}^{(U^{+4})(O^{-2})(O^{-2})} = G_{UO_2}^{UO_2} + G_O^{UO_2}$	$+(y_{Pu^{+3}}-y_{Pu^{+4}})(-17507.47+5.46573T)$
$G_{(U^{+5})(O^{-2})(O^{-2})}^{(MOA)} = G_{(U^{+5})(O^{-2})(Va)}^{(MOA)} + G_{O}^{Sub}$	$L_{(U^{+4},Pu^{+4})(O^{-2})(Va)}^{MOX} = -20000$
$G_{(U^{+3})(Va)(O^{-2})}^{MOX} - H_U^{SER} - H_O^{SER} = G_{(U^{+4})(Va)(O^{-2})}^{MOX} - H_U^{SER} - H_O^{SER}$	$L_{(U^{+4}Pu^{+3})(Q^{-2})(Va)}^{MOX} = -150000$
$=G_{(U^{+5})(Va)(O^{-2})}^{MOX} - H_U^{SER} - H_O^{SER} = +100000$	$L_{(U^{+3},Pu^{+4})(O^{-2})(Va)}^{MOX} = + 20000$
$L_{(U^{+4}, U^{+5})(O^{-2})(O^{-2})}^{MOX} = -124936.9 - 21.6838T$	$L_{(U^{+4},Pu^{+3})(Va)(Va)}^{MOX} = -300000$
$L_{(U^{+3}, U^{+4})(O^{-2})(Va)}^{MOX} = +40133.7 + 1076.4(y_{U^{+3}} - y_{U^{+4}})$	$L_{(Pu^{+4}, U^{+5})(O^{-2})(*)}^{MOX} = -80000$

#### U-0

U-Pu-O

DE LA RECHERCHE À L'INDUSTRIE



#### Nuclear Energy Agency

#### 41 Elements

BETTER POLICIES FOR BETTER LIVES

www.oecd-nea.org/science/taf-id/ (Canada, France, Japan, The

Netherlands, Korea, UK, USA)

206 Binaries





**NEA** 

NUCLEAR ENERGY AGENCY

TAF-ID : Thermody	rAF-ID : Thermodynamics of Advanced Fuels - International Database		
Home     Introduction       Elements     Assessed binary systems       Assessed ternary systems     Higher order systems       Higher order systems     Systems with Ag, Al, Am, Ar       B, Ba, C, Ca, Ce, Cr, Cs, Fe, Gd, H, He, I, La, Mg, Mo, N, Nb, Nd, Ni, Np, O, Pd, Pu, Re, Rh, Ru, Si, Sr     Ta, Tc, Te, Th, Ti, U, V, W, Zr       Periodic table     Periodic table	Nodels     Phases     Systems       Binary systems described by the database       The phase diagrams calculated at 10 <sup>5</sup> Pa for the different assessed binary systems can be displayed thanks to the following list.       Ag-1*     Ag-0*     Ag-1*     Ag-2       Al-Ca     Al-Fe     Al-Fe     Al-Fe     Al-Fe       B-C     B-Cr     B-Fe     Bland     Ba-1     Ba-1       B-C     B-Cr     B-Fe     B.H     B-1     B-1     B-1       B-C     B-Cr     B-Fe     B-H     B-1     C-1     C-1     C-1	Home   Introduction   Models   Phases   Systems     Elements   Assessed binary systems   Assessed ternary systems   Ternary systems     Higher order systems   Systems with Ag, Al, Am, Ar, B, Ba, C, Ca, Ce, Cr, Cs, Fe, Cd, H, He, T, La, Mg, Mo, N, Nb, Nd, Ni, Np, O, Pd, Puu, Re, Rh, Ru, Si, Sr, Ta, T, Ci, Te, Th, Ti, U, V, W, Zr   Ternary systems   Ternary Systems     Periodic table   Ternary Systems   Ba-Moo Da-OU Ba-OZr   Hordo U-N-TI C-N-U C-O-Pu C-O-U C-Pu-U C-Pu-W C-Re-U C-Re-W C-SI-U C-SI-U C-U-W C-I-Zr Ca-SI-U Ca-SI-Zr Ca-SI-U Ca-O-Zr Ca-O-U Mo-O-U Mo-O-D Mo-O-D Mo-O-D Mo-O-Zr Mo-O-U Mo-O-D Mo-O-Zr Mo-O-U Mo-O-Zr Mo-O-U Mo-O-D Mo-O-Zr Mo-O-U Mo-O-Zr Mo-O-U Mo-O-Zr Mo-O-U Mo-O-Zr Ca-O-U Mo-O-D Mo-O-Zr Mo-O-U Mo-O-Zr Mo-D-Zr Mo-O-Zr Mo-O-Zr Mo-O-Zr Mo-O-Zr MO-Zr	

TDB

#### Calculations on irradiated MOX fuel

#### **PREDICTION OF OXYGEN POTENTIAL**

Calculation for a MOX fuel with burnups of 3.8, 7 and 11.2 at .% ⇒ 16 Fission Products (Nd,La,Gd,He,Ce,I,Zr,Cs,Sr,Ba,Te,Mo,Pd,Ru,Tc,Rh)

(U<sup>+3</sup>,U<sup>+4</sup>,U<sup>+5</sup>,Pu<sup>+3</sup>,Pu<sup>+4</sup>,Zr<sup>+2</sup>,Zr<sup>+4</sup>,Ce<sup>+3</sup>,Ce<sup>+4</sup>,Gd<sup>+3</sup>,La<sup>+3</sup>,Nd<sup>+3</sup>)(O<sup>-2</sup>,Va)<sub>2</sub>(O<sup>-2</sup>,Va)



### Calculations on irradiated MOX fuel

#### FORMATION OF SECONDARY FISSION PRODUCT PHASES FOR A 7 at. % BURNUP



# Conclusion

 Thermodynamic modelling of nuclear fuels is required to provide key input thermodynamic and phase diagram data for Fuel Performance Codes

⇒ Oxygen potential, fission product phases (JOG/ROG formation), solid/liquid transitions, heat capacity ....

CALPHAD is a suitable method to model multi-component systems by extrapolating from binary and ternary sub-systems;
⇒ It is time consuming ⇒ International collaborative projects are good frameworks to develop large databases
⇒ Experimental thermodynamic measurements on fuels are challenging but needed to test the validity of the databases (Phase 2 of TAF-ID project)

⇒ First-principle calculations are useful to calculate thermodynamic data that can be used in the models

But thermodynamics (alone) cannot explain the fuel behaviour; it has to be coupled with kinetic and mass transfer models

⇒ In the GERMINAL fuel performance code, there is a coupling using the open source code Open Calphad (developped by Bo Sundman) and the TAF-ID database

- Other Gibbs energy minimizer codes exist such as FACTSAGE, PANDAT, PyCALPHAD ... ⇒ The format of the database can differ; in some cases a conversion of the database file is required (for instance from Thermo-Calc to FACTSAGE format);
  - ⇒ All the sublattice models are not implemeted in all the codes

TAF-ID website: <u>https://www.oecd-nea.org/science/taf-id/</u>

A public version is available ⇒ contact person: davide.costa@oecd.org